# Y2S2 XMQs and MS

(Total: 65 marks)

1.	P3_Sample	Q4	•	10	marks	-	Y2S2	Conditional	probability
2.	P3_Specimen	Q4		11	marks	-	Y2S2	Conditional	probability
3.	P31_2019	Q1		8	marks	-	Y1S5	Probability	
4.	P31_2020	Q1		8	marks	-	Y2S2	Conditional	probability
5.	P31_2021	Q1	•	7	marks	-	Y1S6	Statistical	distributions
6.	P31_2021	Q4	•	11	marks	-	Y2S2	Conditional	probability
7.	P31_2022	Q5	•	10	marks	-	Y2S2	Conditional	probability

4. Given that

$$P(A) = 0.35$$
  $P(B) = 0.45$  and  $P(A \cap B) = 0.13$ 

find

(a)  $P(A' \mid B')$ 

(2)

(b) Explain why the events A and B are not independent.

(1)

The event C has P(C) = 0.20

The events A and C are mutually exclusive and the events B and C are statistically independent.

(c) Draw a Venn diagram to illustrate the events A, B and C, giving the probabilities for each region.

**(5)** 

(d) Find  $P([B \cup C]')$ 

**(2)** 

$= \frac{3}{5} \text{ or } 0.6$ $= \frac{3}{5} \text{ or } 0.6$ (C) $= \frac{3}{5} \text{ or } 0.6$	A1 1.	.1a .1b
(b) e.g. $P(A) \times P(B) = \frac{7}{20} \times \frac{9}{20} = \frac{63}{400} \neq P(A \cap B) = 0.13 = \frac{52}{400}$ or $P(A' \mid B') = 0.6 \neq P(A') = 0.65$ (c) B $\frac{B}{A}$ $0.22$ $0.13$ $0.23$ $0.09$ $0.11$	(2) 31 2	
(b) e.g. $P(A) \times P(B) = \frac{7}{20} \times \frac{9}{20} = \frac{63}{400} \neq P(A \cap B) = 0.13 = \frac{52}{400}$ or $P(A' \mid B') = 0.6 \neq P(A') = 0.65$ (c) B $\frac{B}{A}$ $0.22$ $0.13$ $0.23$ $0.09$ $0.11$	31 2	2.4
or $P(A'   B') = 0.6 \neq P(A') = 0.65$ (c) $B$ $M$ $A$ $0.22$ $0.13$ $0.23$ $0.09$ $0.11$		2.4
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	1)	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		
A 0.22 (0.13) 0.23 (0.09) 0.11	31 2	2.5
A 0.22 (0.13) 0.23 (0.09) 0.11	М1 3.	.1a
	<b>A</b> 1 1.	.1b
	M1 1.	.1b
A	<b>A</b> 1 1.	.1b
	(5)	
(d) $P(B \cup C)' = 0.22 + 0.22 \text{ or } 1 - [0.56]$ or $1 - [0.13 + 0.23 + 0.09 + 0.11]$ o.e.	M1 1.	.1b
= <b>0.44</b> A	<b>A</b> 1 1.	.1b

(10 marks)

#### **Notes:**

(a)

M1: for a correct ratio of probabilities formula and at least one correct value.

**A1:** a correct answer

(b) for a fully correct explanation: correct probabilities and correct comparisons.

(c)

**B1:** for box with B intersecting A and C but C not intersecting A.( Or accept three intersecting circles, but with zeros entered for  $A \cap C$  and  $A \cap B \cap C$ )No box is B0

**M1:** for method for finding  $P(B \cap C)$ 

**A1:** for 0.09

M1: for 0.13 and their 0.09 in correct places and method for their 0.23

A1: fully correct

(d)

**M1:** for a correct expression – ft their probabilities from their Venn diagram.

A1: cao

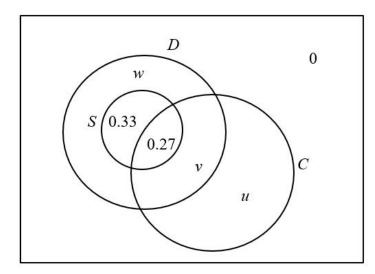
**4.** The Venn diagram shows the probabilities of students' lunch boxes containing a drink, sandwiches and a chocolate bar.

D is the event that a lunch box contains a drink,

S is the event that a lunch box contains sandwiches,

C is the event that a lunch box contains a chocolate bar,

*u*, *v* and *w* are probabilities.



(a) Write down  $P(S \cap D')$  (1)

One day, 80 students each bring in a lunch box. Given that all 80 lunch boxes contain sandwiches and a drink,

(b) estimate how many of these 80 lunch boxes will contain a chocolate bar.

Given that the events S and C are independent and that  $P(D \mid C) = \frac{14}{15}$ 

(c) calculate the value of u, the value of v and the value of w.

(7)

## 9MA0/03 Mock Paper: Statistics and Mechanics mark scheme

Question	Scheme	Marks	AOs
4(a)	$P(S \cap D') = 0$	B1	1.1b
		(1)	
(b)	$P(C   S \cap D) = \frac{0.27}{0.6} = \frac{9}{20} = 0.45$	M1	3.1b
	∴ 80×"0.45"	M1	1.1b
	=36	A1	1.1b
		(3)	
(c)	$[P(C) \times P(S) = P(C \cap S)]$		
	$P(S) = 0.6, P(C) = 0.27 + v + u, P(S \cap C) = 0.27$	M1	3.1a
	$0.6 \times (0.27 + u + v) = 0.27$ or $u + v = 0.18$ o.e	A1	1.1b
	$\left[P(D \mid C) = \frac{P(D \cap C)}{P(C)}\right]  P(D \cap C) = 0.27 + v$	M1	3.1a
	$\frac{14}{15} = \frac{0.27 + v}{0.27 + v + u}$ or $14u - v = 0.27$ o.e	A1	1.1b
	15u = 0.45	M1dd	1.1b
	u = 0.03 $v = 0.15$	A1	1.1b
	w = 0.22	Alft	1.1b
		(7)	

(11 marks)

#### **Notes:**

(a) B1: correct answer only

**(b) M1:** for a correct ratio of probabilities formula with at least one correct value and multiplying by 80

**A1:** a correct answer

(c) M1: for translating the problem and realising the equation  $P(C) \times P(S) = P(C \cap S)$  needs to be used with at least 2 parts correct.

A1: a correct equation

M1: for a correct probability formula with  $P(D \cap C) = 0.27 + v$ 

A1: a second correct equation

**M1dd:** dependent on the previous 2 method marks being awarded. Solving the two simultaneous equations by eliminating one variable. May be implied by either u or v correct

A1: *u* correct

**A1:** *v* correct

**A1ft:** w = 0.22, ft *their* u, v provided that u + v + w < 0.4

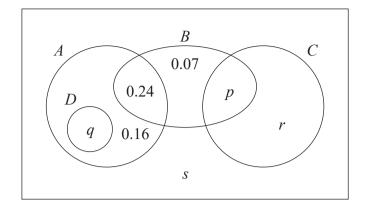
### Answer ALL questions. Write your answers in the spaces provided.

	Answer ALL questions. Write your answers in the spaces provided.	
1.	Three bags, A, B and C, each contain 1 red marble and some green marbles.	
	Bag <i>A</i> contains 1 red marble and 9 green marbles only Bag <i>B</i> contains 1 red marble and 4 green marbles only Bag <i>C</i> contains 1 red marble and 2 green marbles only	
	Sasha selects at random one marble from bag $A$ .  If he selects a red marble, he stops selecting.  If the marble is green, he continues by selecting at random one marble from bag $B$ .  If he selects a red marble, he stops selecting.  If the marble is green, he continues by selecting at random one marble from bag $C$ .	
	(a) Draw a tree diagram to represent this information.	
		(2)
	(b) Find the probability that Sasha selects 3 green marbles.	(2)
	(c) Find the probability that Sasha selects at least 1 marble of each colour.	(2)
	(d) Given that Sasha selects a red marble, find the probability that he selects it from bag	B. (2)



Question	Scheme	Marks	AOs				
1(a)	$\frac{2}{3}$ G	B1	1.1b				
	$ \begin{array}{c c} \frac{9}{10} & G & \frac{1}{3} & R \\ \hline \frac{1}{5} & R &  \end{array} $	dB1	1.1b				
	$\frac{1}{10}$ R						
<b>(b)</b>	$\frac{9}{10} \times \frac{4}{5} \times \frac{2}{3}$	M1	1.1b				
	$=\frac{12}{25}(=0.48)$	A1	1.1b				
		(2)					
(c)	$\frac{9}{10} \times \frac{1}{5} + \frac{9}{10} \times \frac{4}{5} \times \frac{1}{3}$ or $1 - \left(\frac{1}{10} + \frac{9}{10} \times \frac{4}{5} \times \frac{2}{3}\right)$	M1	3.1b				
	$=\frac{21}{50}$ (= 0.42)	A1	1.1b				
		(2)					
(d)	[P(Red from B Red selected)] = $\frac{\frac{9}{10} \times \frac{1}{5}}{\frac{1}{10} + \frac{9}{10} \times \frac{1}{5} + \frac{9}{10} \times \frac{4}{5} \times \frac{1}{3}} = \frac{\frac{9}{50}}{\frac{13}{25}}$	M1	3.1b				
	$=\frac{9}{26}$	A1	1.1b				
		(2)					
	Natas	()	8 marks)				
	Notes  Allow decimals or percentages throughout this of	uestion.					
(a)	dB1: (dep on previous B1) all correct i.e. for all 6 correct probabilities on the						
(b)	correct branches with at least one label on <b>each</b> pair  M1: Multiplication of 3 correct probabilities (allow ft from their tree diagram)  A1: $\frac{12}{25}$ oe						
(c)	<b>M1:</b> Either addition of only two correct products (product of two probs + product of three probs) which may ft from their tree diagram						
(d)	M1: Correct ratio of probabilities or correct ft ratio of probabilities e.g. $\frac{\frac{9}{10} \times \frac{1}{5}}{1 - \frac{1}{10}}$ or $\frac{\frac{9}{10} \times \frac{1}{5}}{\frac{1}{10}}$ or $\frac{\frac{9}{10} \times \frac{1}{5}}{\frac{1}{10}}$ (allow awrt 0.346)	with nun	n < den				

1. The Venn diagram shows the probabilities associated with four events, A, B, C and D



(a) Write down any pair of mutually exclusive events from A, B, C and D

**(1)** 

Given that P(B) = 0.4

(b) find the value of p

(1)

Given also that A and B are independent

(c) find the value of q

**(2)** 

Given further that P(B'|C) = 0.64

- (d) find
  - (i) the value of r
  - (ii) the value of s

**(4)** 

2

Qu 1	Scheme	Marks	AO	
(a)	$A, C  \underline{\text{or}}  D, B  \underline{\text{or}}  D, C$	B1	1.2	
(b)	[p = 0.4 - 0.07 - 0.24 = ] <b>0.09</b>	B1 (1)	1.1b	
(c)	A and B independent implies	(1)	1.1b	
	$P(A) \times 0.4 = 0.24$ or $(q+0.16+0.24) \times 0.4 = 0.24$	M1		
	so $P(A) = 0.6$ and $q = 0.20$	Alcso	1.1b	
		(2)		
(d)(i)	$P(B' C) = 0.64$ gives $\frac{r}{r+p} = 0.64$ or $\frac{r}{r+"0.09"} = 0.64$ r = 0.64r + 0.64 "p" so $0.36r = 0.0576$ so $r = 0.16$	M1	3.1a	
	r = 0.64r + 0.64 "p" so $0.36r = 0.0576$ so $r = 0.16$	A1	1.1b	
		3.54		
(ii)	Using sum of probabilities = 1 e.g. " $0.6$ " + $0.07$ + " $0.25$ " + $s$ = 1	M1	1.1b	
	so $s = 0.08$	A1 (4)	1.1b	
		(4)		
		(8 mark	(s)	
(a)	Notes			
(a)	B1 for one correct pair. If more than one pair they must all be correct. Condone in a correct probability statement such as $P(A \cap C) = 0$			
	or correct use of set notation e.g. $A \cap C = \emptyset$			
	BUT e.g. " $P(A)$ and $P(C)$ are mutually exclusive" alone is B0			
(b)	B1 for $p = 0.09$ (Maybe stated in Venn Diagram [VD]) [ If values in VD and text conflict, take text or a value <u>used</u> in a later part]			
(c)	M1 for a correct equation in one variable for $P(A)$ or $q$ using indep	endence		
	or for seeing <b>both</b> $P(A \cap B) = P(A) \times P(B)$ and $0.24 = 0.6 \times 0$ .			
	A1cso for $q = 0.20$ or exact equivalent (dep on correct use of independent)	ndence)		
Beware	Use of $P(A) = 1 - P(B) = 0.6$ leading to $q = 0.2$ scores M0A0			
(d)(i)	1 <sup>st</sup> M1 for use of $P(B'   C) = 0.64$ leading to a correct equation in $r$ and possibly $p$ .			
	Can ft their $p$ provided $0$			
(ii)	$1^{st}$ A1 for $r = 0.16$ or exact equivalent $2^{nd}$ M1 for use of total probability = 1 to form a linear equation in s. A	llow <i>n. a.</i>	r etc	
	Can follow through their values provided each of $p$ , $q$ , $r$ are in		7 010	
	$2^{\text{nd}} \text{ A1}$ for $s = 0.08$ or exact equivalent			

**1.** (a) State one disadvantage of using quota sampling compared with simple random sampling.

**(1)** 

In a university 8% of students are members of the university dance club.

A random sample of 36 students is taken from the university.

The random variable *X* represents the number of these students who are members of the dance club.

- (b) Using a suitable model for *X*, find
  - (i) P(X = 4)
  - (ii)  $P(X \ge 7)$

**(3)** 

Only 40% of the university dance club members can dance the tango.

(c) Find the probability that a student is a member of the university dance club and can dance the tango.

**(1)** 

A random sample of 50 students is taken from the university.

(d) Find the probability that fewer than 3 of these students are members of the university dance club and can dance the tango.

**(2)** 



Qu 1	Scheme Marks AO					
(a)	Disadvantage: e.g. Not random; cannot use (reli	ably) for inferences	B1	1.1b		
			(1)			
<b>(b)</b>	[Sight or correct use of] $X \sim B(36, 0.08)$		M1	3.3		
(i)	P(X = 4) = 0.167387 aw		A1	1.1b		
(ii)	$[P(X \geqslant 7) = 1 - P(X \leqslant 6) =] 0.0$	A1	1.1b			
			(3)			
(c)	P(In dance club and dance tango) = $0.4 \times 0.08 = 0.4 \times 0.08$	B1	1.1b			
		(1)				
(d)	[Let $T =$ those who can dance the Tango. Sight or	M1	3.3			
	$[P(T < 3) = P(T \le 2) = ]  0.7850815$	A1	1.1b			
		(2)				
	<b>X</b>	(7 marks)				
(-)	Note	es				
(a)						
	Allow (B1)  Not random or less random (o.e.)  Cannot use (reliably) for inferences  Do NOT allow (B0)  Not representative  Less accurate					
	`	ne or cost				
		c or cost				
		Any mention of skew  Any mention of non-respon	se			
	This manner of non-response					
(b)	M1 for sight of B(36, 0.08) Allow in words: <u>binomial</u> with $\underline{n} = 36$ and $\underline{p} = 0.08$ may be implied by one correct answer to 2sf <u>or</u> sight of P( $X \le 6$ ) = 0.97776 i.e. awrt 0.98 Allow for $36C4 \times 0.08^4 \times 0.92^{32}$ as this is "correct use"					
(i)		awrt $0.167$ scores $M1(\Rightarrow)$	1 <sup>st</sup> A 1			
(ii)	2 <sup>nd</sup> A1 for awrt 0.0222	tunit 0.107 scores mil(=)	1 711			
(c)	B1 for $0.032$ o.e. (Can allow for sight of $0.4 \times 0.08$ )					
(-)						
(d)	M1 for sight of B(50, "0.032") ft their answer to may be implied by correct answer					
MR	or sight of $[P(T \le 3)] = 0.924348$ i.e. awrt 0. A1 for awrt 0.785 Allow MR of 50 (e.g. 30) provided clearly a	_		2) calc.		
	, <i>b</i> /1					

**4.** A large college produces three magazines.

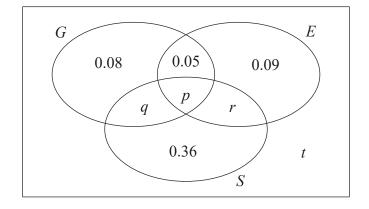
One magazine is about green issues, one is about equality and one is about sports. A student at the college is selected at random and the events G, E and S are defined as follows

G is the event that the student reads the magazine about green issues

E is the event that the student reads the magazine about equality

S is the event that the student reads the magazine about sports

The Venn diagram, where p, q, r and t are probabilities, gives the probability for each subset.



(a) Find the proportion of students in the college who read exactly one of these magazines.

**(1)** 

No students read all three magazines and P(G) = 0.25

- (b) Find
  - (i) the value of p
  - (ii) the value of q

**(3)** 

Given that  $P(S \mid E) = \frac{5}{12}$ 

- (c) find
  - (i) the value of r
  - (ii) the value of t

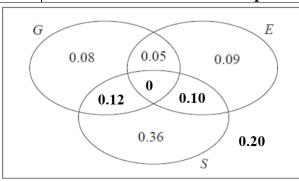
**(4)** 

(d) Determine whether or not the events  $(S \cap E')$  and G are independent. Show your working clearly.

**(3)** 



Qu 4	Scheme	Marks	AO		
(a)	$0.08 + 0.09 + 0.36 = \underline{0.53}$	B1	1.1b		
		(1)			
(b)(i)	$\left[P(G \cap E \cap S) = 0 \Rightarrow\right] \underline{p} = 0$	B1	1.1b		
(ii)	$[P(G) = 0.25 \implies] 0.08 + 0.05 + q + "p" = 0.25$	M1	1.1b		
	q = 0.12	A1	1.1b		
(a)(i)		(3)	2.1		
(c)(i)	$P(S \mid E) = \frac{5}{12} \implies \frac{r + p}{r + p + 0.09 + 0.05} = \frac{5}{12}$	M1 A1ft	3.1a 1.1b		
	$\begin{bmatrix} 12r = 5r + 5 \times 0.14 \implies \end{bmatrix}  \underline{r} = 0.10$	A1	1.1b		
(ii)	$[0.08 + 0.05 + "0.12" + "0" + 0.09 + "0.10" + 0.36 + t = 1 \implies] t = 0.20$	B1ft	1.1b		
		(4)			
( <b>d</b> )	$P(S \cap E') = 0.36 + "q" [= 0.48]$	B1ft	1.1b		
	$P((S \cap E') \cap G) = "q" = 0.12$ and $P(G) = 0.25$ and				
	$P(S \cap E') \times P(G) = "0.48" \times \frac{1}{4} \text{ or } 0.12$	M1	2.1		
	•				
	$P(S \cap E') \times P(G) = 0.12 = P([(S \cap E')] \cap G)$ so are independent	A1	2.2a		
		(3) (11 mar)	za)		
	Notes	( 11 mai)	NS)		
(a)	B1 for 0.53 (or exact equivalent) [ Allow 53%]				
( <b>b</b> .)( <b>!</b> )	D1 for a O(more he alooed in Venn diagram)				
(b)(i) (ii)	B1 for $p = 0$ (may be placed in Venn diagram) M1 for a linear equation for $q$ (ft letter " $p$ " or their value if $0 \le p \le 0.12$ ) =	$\Rightarrow$ by $p+a=$	= 0.12		
	A1 for $q = 0.12$ (may be placed in Venn diagram)				
(2)(2)	M1 for a notic of muchabilities (non-new and day) (and HIG) and	L	d		
(c)(i)	M1 for a ratio of probabilities ( $r$ on num and den) (on LHS) with num < den correct ft. Allow ft of letter " $p$ " or their $p$ where $0 \le p < 0.86$ but " $+$ 0"				
	$1^{\text{st}}$ A1ft for a correct ratio of probabilities (on LHS) allowing ft of their $p$ when	-			
	$2^{\text{nd}}$ A1 for $r = 0.1(0)$ or exact equivalent (may be in Venn diagram) <b>Ans only</b>	y 3/3			
(ii)	B1ft for $t = 0.2(0)$ (o.e.) or correct ft i.e. $0.42 - (p + q + r)$ where $p, q, r$ are	nd t are all	probs		
(d)	B1ft for $P(S \cap E') = 0.48$ (with label) (ft letter "q" or their value if $0 \le q \le$	(0.12)			
	M1 for attempting all required probs (labelled) and using them in a correct tes		of $q$ )		
	A1 for all probs correct and a correct deduction (no ft deduction here)	•	•		
SC	No "P" If correct argument seen apart from P for probability for all 3 marks, a	,			
L	If unsure about an attempt using conditional probabilities, please sen	u to reviev	<b>W</b> •		



**5.** A company has 1825 employees.

The employees are classified as professional, skilled or elementary.

The following table shows

- the number of employees in each classification
- the two areas, A or B, where the employees live

	A	В
Professional	740	380
Skilled	275	90
Elementary	260	80

An employee is chosen at random.

Find the probability that this employee

(a) is skilled,

**(1)** 

(b) lives in area B and is not a professional.

**(1)** 

Some classifications of employees are more likely to work from home.

- 65% of professional employees in both area A and area B work from home
- 40% of skilled employees in both area A and area B work from home
- 5% of elementary employees in both area A and area B work from home
- Event F is that the employee is a professional
- Event *H* is that the employee works from home
- Event R is that the employee is from area A
- (c) Using this information, complete the Venn diagram on the opposite page.

(4)

(d) Find  $P(R' \cap F)$ 

**(1)** 

(e) Find  $P([H \cup R]')$ 

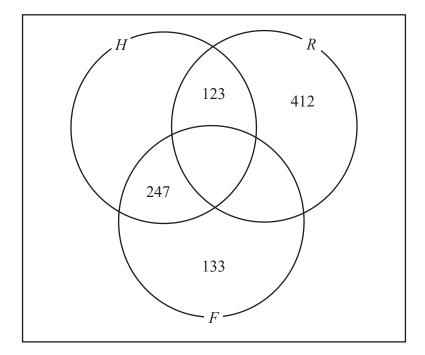
**(1)** 

(f) Find  $P(F \mid H)$ 

**(2)** 



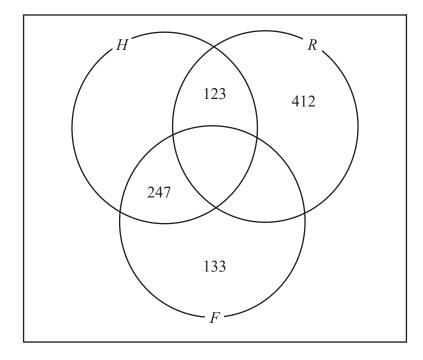
## **Question 5 continued**



Turn over for a spare diagram if you need to redraw your Venn diagram.


## **Question 5 continued**

Only use this diagram if you need to redraw your Venn diagram.



(Total for Question 5 is 10 marks)



Quest	ion	Scheme	Marks	AOs				
5(a	)	$\frac{365}{1825}$ or $\frac{1}{5}$ or 0.2 oe	B1	1.1b				
		1825 5	(1)					
(b)	)	170 34						
(~)	•	$\frac{170}{1825}$ or $\frac{34}{365}$ or awrt 0.093	B1	1.1b				
(c)			(1)					
		$90 \times 0.4 + 80 \times 0.05 = 40$ or $90 \times 0.6 + 80 \times 0.95 = 130$ or	M1	3.1b				
		$740 \times 0.65 = 481$ or $740 \times 0.35 = 259$	1711	3.10				
		H 40 123 412 R 481 247 259 133 F 130	B1 B1 A1	1.1b 1.1b 1.1b				
			(4)					
(d)		$P(R' \cap F) = \frac{380}{1825} \left[ = \frac{76}{365} = 0.208 \right]$ oe awrt 0.208	B1	1.1b				
		1823	(1)					
(e)		$\left[\frac{133 + "130"}{} = \right] \frac{"263"}{}$ awrt 0.144	B1ft	1.1b				
		L 1825		1.10				
<b>(</b>		247 : !! 401!!	(1)					
<b>(f)</b>		247 + "481" 247 + "481" + 123 + "40"	M1	3.4				
		$=\frac{728}{}$ awrt 0.817	A 1	1 11				
		$-\frac{891}{891}$	A1	1.1b				
			(2)					
		Notes:		narks)				
		Look out for answers given in the question. If you see answers in the in the answer space those in the answer space take precedence.	ne questioi	ı anu				
(a)	B1	Allow equivalent						
(b)	B1	Allow equivalent						
	M1	Correct method to find one of the values 40 or 130 or 481or 259						
(c)	1811	Implied by 40, 481, 259 or 130 seen in correct place on diagram						
	B1	One of the highlighted correct						
	B1	A second value highlighted correct or their $("259"+"481") = 740$ or						
		their $("40"+" 481") = 521$ or their $("40"+"130") = 170$						
	A1	Fully correct						
(d)	B1	380/1825oe or awrt 0.208						
(e)	B1ft	Ft their 130 (>0) do not allow if blank Allow ft correct to 3 sf.	Correct answer or Ft their 130 ( > 0) do not allow if blank					
<b>(f)</b>	M1	For a single fraction with the numerator $<$ denominator and $n$ is an int award for $n/891$ or $n/(\text{sum of their 4 values in } H$ , each $> 0)$ or awrt		i11 				
	A1	award for $n/891$ or $n/(80m)$ of their 4 values in $H$ , each > 0) or awrt 0.81 / 728/891 oe or awrt 0.817						